temperature differences exist between the day and night faces of the planet, consistent with a model in which very little horizontal energy transport occurs in the planetary atmosphere. Furthermore, it indicates that the opportunities for direct extrasolar planetary observations are better than previously thought, because useful data can be obtained even in cases where the planetary orbit is not so fortuitously aligned that the system exhibits transits or eclipses.

References and Notes
3. There is no official terminology for planets that orbit close to their parent stars. The term "hot Jupiter" is the most common, although some authors have adopted other terms, such as "Pegasi planets," "Pegasi planets," or "Rotasters.
8. The passage of an extrasolar planet behind its star, an eclipse, results in a drop in the total system flux. This allows a measurement of the absolute flux emerging from the part of the planet that faces the star (the day side). This is possible when the orbit is aligned almost edge-on to the line of sight.
10. We use the estimator provided by the Spitzer Science Center, which is based on the DIRBE model described by (21). Further information on the specific implementation is given at http://ssc.spitzer.caltech.edu/documents/background.
22. The usual estimate given for planetary temperatures is the equilibrium temperature, $T_{eq}$, defined as the effective temperature of a uniformly bright planet radiating energy at a rate that balances the irradiation received from the star, $T_m$, is thus determined by the stellar effective temperature, $T_{m}$, and distance of the planet from the star $a$:

$$ T_{m} = \frac{1744 \, K \, T_{eq} / 6212 \, K \, (R_{\ast} / 1.57 \, R_{\odot})^{3/2} \times (a/0.059 \, AU)^{1/2}} $$

in the case of $u$ and $b$ with albedo $=0.05$. However, in a proper non-redistribution model, the temperature distribution is not uniform but rather hottest at the substellar point and coolest at the limb, and the full-phase temperature average over the planetary surface is better approximated by $(\tan u - \tan b)/2$. This is the temperature we adopt, which is 1875 K in this case.
23. This work is based on observations made with the Spitzer Space Telescope, which is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with NASA. Support for this work was provided directly by NASA, its Origins of Solar Systems and Astrophysical Theory programs, as well as the Astrobiology Institute and Spitzer Science Center. We thank the personnel of the Spitzer Science Center and its MIPS instrument, who ultimately made these measurements possible.

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Brownian Motion of an Ellipsoid

Y. Han, A. M. Alsayed, M. Nobili, Zhang, T. C. Lubensky, A. G. Yodh

We studied the Brownian motion of isolated ellipsoidal particles in water confined to two dimensions and elucidated the effects of coupling between rotational and translational motion. By using digital video microscopy, we quantified the crossover from short-time anisotropic to long-time isotropic diffusion and directly measured probability distributions functions for displacements. We confirmed and interpreted our measurements by using Langevin theory and numerical simulations. Our theory and observations provide insights into fundamental diffusive processes, which are potentially useful for understanding transport in membranes and for understanding the motions of anisotropic macromolecules.

Brownian motion (1), wherein small particles suspended in a fluid undergo continuous random displacements, has fascinated scientists since before it was first investigated by the botanist Robert Brown in the early 19th century. The origin of this mysterious motion was largely unexplained until Einstein's famous 1905 paper (2) that established a relation between the diffusion coefficient of a Brownian particle and its friction coefficient. One year later (3), Einstein extended the concept of Brownian dynamics to rotational and other degrees of freedom. The subsequent study of Brownian motion and its generalizations has had a profound impact on physics, mathematics, chemistry, and biology (4). Because direct detection of translational Brownian motion is relatively easy, many experiments elucidating the ideas of translational diffusion have been carried out. On the other hand, the direct visualization of rotational Brownian motion has not been an easy task, and fundamental concepts about motions of anisotropic macromolecules remain untested. For this contribution, we used digital video microscopy to study the Brownian motion of an isolated ellipsoid in suspension and thus directly observed the coupling effects between rotational and translational motion.

Particle anisotropy leads to dissipative coupling of translational to rotational motion and to physics first explored by F. Perrin (5, 6). A uniaxial anisotropic particle is characterized by two translational hydrodynamic friction coefficients, $\gamma_a$ and $\gamma_b$, respectively, for motion parallel and perpendicular to its long axis. If a particle's rotation is prohibited, it will diffuse independently in directions parallel and perpendicular to its long axis. If the rotation is allowed, rotational diffusion, characterized in two dimensions by a single diffusion coefficient, $D_a$, and associated diffusion time, $t_0 = 1/(2D_a)$, washes out directional memory and leads to a crossover from anisotropic diffusion at short times to isotropic diffusion at times much longer than $t_0$. Figure 1, A and B, presents numerical simulations (8) that illustrate this behavior. Our experiments, which were restricted to two dimensions (2D), provide explicit verification of this behavior and some of its extensions. In addition, we show that a fundamental property of systems with dissipatively coupled translation and rotation is the existence of non-Gaussian probability density functions (PDFs) for displacements in the lab frame.

Micrometer-sized PMMA (polymethyl methacrylate) uniaxial ellipsoids (9) were under strong quasi-two-dimensional confinement in a thin glass cell. The choice of 2D rather than 3D for these studies substantially simplified the experimental imaging tasks as well as the data acquisition time and storage requirements. The choice also ensured that the measured effects would be large by virtue of the much larger friction anisotropy in 2D compared with 3D. The local cell thickness was $\sim 1 \mu m$. It was measured to within 0.1 $\mu m$ resolution by comparing the Michel-Levy chart (10) to the reflected interference colors produced by the two inner surfaces under white light illumination on the microscope (Fig. 1D). To avoid interactions between ellipsoids, we made the solution very dilute. The Brownian motion of a single ellipsoid in water was recorded by a charge-coupled device (CCD) camera on a videotape at 30 frame/s. From the image analyses, we obtained data sets consisting of a particle's center-of-mass positions and velocities.
x(t_n) = [x(t_n), y(t_n)] \) in the lab frame and its orientation angles \( \theta(t_n) \) relative to the x axis at times \( t_n = n(1/30) \) s, as shown in Fig. 1F. The orientational resolution is 1°, and spatial resolutions are 0.5 pixel = 40 nm along the particle's short axis and only 0.8 pixel along its long axis because of the superimposed small tumbling motion. We define each 1/30-s time interval as a step. During the \( n \)th step, the particle's position changes by \( \Delta x(t_n) = x(t_n) - x(t_{n-1}) \) and its angle by \( \Delta \theta(t_n) = \theta(t_n) - \theta(t_{n-1}) \). From the data set, we extract an ensemble of particle trajectories starting at different times \( t_0 \) and ending a time \( t \) later. The total positional and angular displacements in these trajectories are, respectively, \( \Delta x(t) = x(t + \tau_0) - x(\tau_0) \) and \( \Delta \theta(t) = \theta(t + \tau_0) - \theta(\tau_0) \).

We first consider the statistical properties of \( \theta(t) \), which, as pointed out by Perrin (6), are independent of translational motions. We measured data from a 30-min trajectory of a 2.4 \( \mu \)m by -0.3 \( \mu \)m by -0.3 \( \mu \)m ellipsoid confined in an 846-nm-thick cell (Fig. 2A). The inset shows that the mean-square angular displacement \( \langle \Delta \theta(t)^2 \rangle \) equals \( 2 D_{\theta} t \), where the average \( \langle \cdot \rangle \) is over all trajectories with different starting times \( t_0 \). The mean-square angular displacement has diffusive behavior over the entire range of observable times with a rotational time of \( t_{\theta} = 1/(2 D_{\theta}) = 3.1 \) s. Over the time scales we can observe, this diffusive behavior is independent of \( \theta_0 \). The PDF for \( \Delta \theta(t) \) was measured to be Gaussian with variance \( 2 D_{\theta} t \), and the angles \( \theta(t) \) were measured to be uniformly distributed in \([0, 2\pi]\).

We now turn to the statistics of translational motion whose full understanding is facilitated by the consideration of decomposing the displacement \( \Delta x \) into its components \( \Delta x_n \) relative to the body frame or \( \Delta x_{\bar{n}} \) relative to the fixed lab frame. As shown in Fig. 1C, the two are related via a rotation, \( \delta x_{\bar{n}} = R_{ij} \delta x_n \), where the Einstein summation convention on repeated indices is understood and \( R_{ij} = (\cos \theta, \sin \theta, -\sin \theta, \cos \theta) \) is the rotation matrix with \( \theta_0 = (\theta(t_{n-1}) + \theta(t_n))/2 \). In practice, choosing \( \theta_0 = \theta(t_{n-1}) \) or \( \theta_0 = \theta(t_n) \) has little effect on our results because \( \theta \) barely changes during 1/30 s.

We can construct total body-frame displacements by summing over displacements in each step, \( \Delta \bar{x}(t) = \sum_{n=0}^{\infty} \delta \bar{x}_n \), and from \( \Delta \bar{x}(t) \) we can construct body-frame displacements for trajectories of duration \( t \) at starting time \( t_0 \) via \( \Delta \bar{x}(t) = \bar{x}(t + \tau_0) - \bar{x}(\tau_0) \).

Mean-square displacements (MSDs) in the body frame and in the lab frame were averaged over all trajectories with different initial angle \( \theta_0 = \theta(t_0) \) (Fig. 2A). They are all diffusive with \( \langle \Delta \bar{x}(t)^2 \rangle = 2 D_{x} t \), \( \langle \Delta \bar{y}(t)^2 \rangle = 2 D_{y} t \), and \( \langle \Delta \theta(t)^2 \rangle = 2 D_{\theta} t \). The full average \( \langle \cdot \rangle \) over all \( \theta_0 \); \( \langle A \rangle = [\langle A \rangle_0]_0 = \frac{1}{2} \sum_{i,j} G_{ij} \theta_{ij}(A) \theta_{ij} \),

where a particle with a given initial angle will diffuse more rapidly along its long axis than along its short axis. As time progresses, however, memory of its initial direction is lost, and diffusion becomes isotropic. Thus, averages over trajectories at fixed \( \theta_0 \) should exhibit a crossover from early-time anisotropic to late-time isotropic diffusion. Our measurements with \( \theta_0 = 0 \) of the time-dependent diffusion coefficients \( D_{\bar{x}}(t) = \langle \Delta \bar{x}(t)^2 \rangle/2t \) and \( D_{\bar{y}}(t) = \langle \Delta \bar{y}(t)^2 \rangle/2t \) provide direct verification of this crossover (Fig. 2B): At \( t < t_{\theta} \), \( D_{\bar{x}} \) equals \( D_x \) and \( D_{\bar{y}} \) equals \( D_y \), whereas for \( t > t_{\theta} \) \( D_{\bar{x}} \) equals \( D_x \) and \( D_{\bar{y}} \) equals \( D_y \).

The anisotropic-to-isotropic crossover was calculated in 3D by Perrin (6) and is mentioned in qualitative terms in a 3D simulation (11). We calculate the properties of this transition in 2D within the Langevin formalism and compare them with experiment. Because our time scales are much larger than the momentum relaxation times of a micrometer-sized particle in water (\( \Delta \bar{x} \sim m/2\Delta \sim 10^{-7} \) s), we can ignore inertial terms. The Langevin equations for displacement and angle in the lab frame in the presence of external forces described by a Hamiltonian \( H \) are

\[
\begin{align*}
\dot{\delta x}_n &= -\Gamma_{x}(t) \frac{\partial H}{\partial \delta x}_n + \zeta_n(t) \\
\dot{\delta \theta} &= -\Gamma_{\theta}(t) \frac{\partial H}{\partial \delta \theta} + \zeta_{\theta}(t)
\end{align*}
\]

where \( i = x, y \) for 2D and \( \Gamma_{ij} = \gamma^{-1} \) is the mobility tensor, which can be expressed in terms of the unit vector \( \hat{u}(t) = u(t) \) specifying the direction of the local anisotropy axis as \( \Gamma_{ij} = \sum_{n=0}^{\infty} \Delta \bar{n}(n(t)) \gamma_{ij} + \Delta \bar{n}(n(t)) \gamma_{ij} + \Delta M(n(t)) \gamma_{ij}/2 \), where \( \gamma(\Delta \bar{x}) = \Gamma_{\bar{x}} \), \( \Delta \bar{x} = \Gamma_{\bar{x}} = \Gamma_{\bar{y}} = \Gamma_{\bar{z}} \), and \( M(n(t)) = \begin{pmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & -\cos 2\theta \end{pmatrix} \). \( \hat{u}(t) \) and \( \zeta_{\theta}(t) \) are random...
dom noise sources with zero mean and respective variances, \( \zeta_{\text{DIR}}(t) = 2k_B T \delta(t - t_f) = 2k_B \delta(t - t_f) \), dictated by the Einstein relation or equivalently by the requirement that thermal equilibrium be reached at long times. We retain \( H \) in Eq. 1 even though the external forces are zero in our experiments to emphasize that the mobilities \( \Gamma_{xy} \) and \( \Gamma_x \) relating velocity and angular velocity to force and torque, respectively, determine the variances of the random noise sources, \( \xi(t) \) obeys Gaussian statistics at all times, as does \( \zeta(t) \) for a fixed angle \( \theta \). The average \( \langle \xi \rangle_{\theta_0} \) of any measurable quantity is equivalent to the average of \( A \) over both \( \xi(t) \) and \( \zeta(t) \) at fixed \( \theta_0 \).

Because there are no external forces in our experiments, we can set \( \partial H / \partial \phi = 0 \) and \( \partial H / \partial \omega = 0 \). Equation 1b for \( \theta(t) \) is simply the Langevin equation for 1D diffusion. It yields a time-dependent diffusion coefficient \( D_{\theta}(t) \), a Gaussian PDF for \( \Delta \theta(t) \) with variance \( 2 D_{\theta}(t) \), and consequently \( \cos (\Delta \theta(t)) = \text{Re}(e^{i \Delta \theta(t)}) \). From this we can calculate (8) the time-dependent displacement diffusion tensor for fixed \( \theta_0 \):

\[
D_{\theta}(t, \theta_0) = \frac{\langle \Delta \theta(t) \rangle_{\theta_0}^2 / 2}{D_{\theta}(t, \theta_0)}
\]

where \( D_{\theta}(t) \) is the diffusion coefficient for \( \theta(t) \), and \( \Delta \theta(t) = \int_0^t dt' e^{-t' t_{\phi}} \langle \Delta \theta(t) \rangle_{\theta_0} \), and \( \Delta \theta(t) \) quantitatively match experimental results for \( \theta_0 = 0 \) as shown in Fig. 2B, with \( D_{\phi} \) and \( D_{\theta} \) equal to their values obtained from Fig. 2A. The average of \( D_{\theta}(t, \theta_0) \) in Eq. 2 over initial angles \( \theta_0 \) yields \( D_{\phi} = D_{\theta} = D \), in agreement with the MSDs of \( x \) and \( y \) in Fig. 2A. The 3D counterpart, \( D_x = D_y = D_z = \langle \Delta \theta(t) \rangle_{\theta_0}^2 / 2D \), is widely used in dynamic light scattering (12).

Unlike spheres, anisotropic particles have anisotropic friction coefficients that are responsible for the coupling of translation and rotation.

This coupling leads to nontrivial mixed correlation functions such as

\[
\sigma(\Delta t; \Delta x e^{i \omega_0 t}) / j = 2D + \Delta D_{\phi} \langle \Delta \phi(t) \rangle_{/2} e^{i \Delta \phi(t)} - e^{i \omega_0 t} \]

where \( \Delta D_{\phi} \approx e^{i \omega_0 (\Delta \phi(t) / 2)} - e^{i \omega_0 (\Delta \phi(t) / 2)} \). Mixed correlations of translational displacements \( \langle \Delta x(t) \rangle_{\phi} \) and \( \langle \Delta y(t) \rangle_{\phi} \) is Gaussian with zero mean and variance \( \langle \Delta x(t) \rangle_{\phi} = 2k_B T \langle \Delta y(t) \rangle_{\phi} \) equals \( 2D t \), where \( D \) is the friction coefficient and \( \Delta \phi(t) \) is the internal angle. In agreement with the experimental data in Fig. 2A. Because \( \Delta \phi(t) \) is Gaussian, the PDF for body-frame displacements \( \Delta \phi(t) \) is Gaussian at all times:

\[
f_\phi(x, \phi_0) = \frac{1}{\sqrt{2\pi \sigma_\phi^2(\phi_0)}} e^{-x^2 / 2 \sigma_\phi^2(\phi_0)}
\]

where \( \sigma_\phi^2 = 2D t \). Our measurements confirm this behavior in fig. S1. For our quasi-2D sample, the ellipsoid's friction and diffusion tensors are different at different heights within the cell (13). Therefore, the PDF of \( \Delta \phi(t) \) should be an average of Gaussian PDFs with different variances. However, the interference color from the ellipsoid changed very little throughout the course of our experiment, from this result we estimate that the ellipsoid remains within 50 nm of the midpoint of the cell and that the non-Gaussian effects are too small to be observable as is confirmed by our measurements.

Although the statistics of displacements in the body frame are Gaussian, those in the lab frame are not because of coupling between translation and rotation. Prager (15) calculated the non-Gaussian concentration for averaged initial angles in a particular geometry in three dimensions. The lab-frame noise, \( \xi(t) = R_{\phi}^{-1} \xi(t) \), is a linear function of the independent noises \( \xi(t) \) and \( \xi(t) \). Thus, although its probability distribution is Gaussian for fixed \( \theta(t) \) and thus fixed \( \xi(t) \), its distribution averaged over \( \xi(t) \) is non-Gaussian, as is that for \( \Delta x(t) \). At short times, the lab- and body-frame displacements are equal, and the PDF for \( \Delta x(t) \) is Gaussian because that for \( \Delta x(t) \) is. Directional information is lost at times greater than \( t_0 \). Therefore, at long times, \( \Delta x(t) \) is a sum of displacements from \( -\xi \) statistically independent steps, and the central limit theorem implies that its PDF is Gaussian. Thus at fixed \( \theta_0 \), we expect deviation from Gaussian behavior to vanish at \( t = 0 \) and \( t = \infty \) and to reach a maximum at times of order \( t_0 \).

The simplest manifestations of non-Gaussian behavior are the nonzero values of the fourth- or higher-order cumulants of lab-frame displacements, which can be calculated (8) from our Langevin theory. For example, the fourth cumulant of \( \Delta \phi(t) \) for fixed initial orientation is

\[
C_4 (\phi(t)) = \left( \langle \Delta x(t) \rangle \right)^4_{\phi} / 3 \left( \langle \Delta \phi(t) \rangle \right)^2_{\phi}
\]

\[
= \frac{1}{2} \left( \Delta D \right)^2 \left[ 3 \langle \Delta \phi(t) \rangle - \langle \Delta \phi(t) \rangle \right]
\]

\[
+ \left[ \langle \Delta \phi(t) \rangle - \langle \Delta \phi(t) \rangle - 3 \langle \Delta \phi(t) \rangle \right] \cos \theta_0
\]

\[
(6)
\]

**Fig. 2.** (A) MSDs along \( a, b, x, \) and \( y \) axes. (Inset) Angular MSD. All curves have diffusive behavior \((< 1)\), and corresponding diffusion coefficients \( D = \) MSD/2D shown in the figure are from best fits. (B) Diffusion coefficients \( D \) in the lab frame. The initial orientation of each trajectory was chosen to be along the \( x \) axis \((\theta_0 = 0)\), so that \( D_{xx} \) and \( D_{yy} \) change from \( D_a \) and \( D_b \) to \( D \), respectively, over time interval \( t_0 \). Symbols, experiment; error bars \( \propto \sqrt{t} \). Solid curves, Eq. 2 when \( \theta_0 = 0 \). (C) Mixed correlations of translational displacements and orientation. Symbols, experiment. Error bars \( \propto \sqrt{t} \). Solid curves, theoretical results from Eq. 3 for \( n = 2 \). Dashed curves, reference uncorrelated averages \( \langle \Delta x^2 \rangle \cos \theta(t) / t \), \( \langle \Delta y^2 \rangle \cos \theta(t) / t \), and \( 2 \langle \Delta x \Delta y \rangle \sin \theta(t) / t \).
This function vanishes as $t^{2+2s}$, where $s_2 > 0$, as $t \to 0$ and grows linearly in $t$ as $t \to \infty$. The non-Gaussian parameter,

$$p(t, \theta_0) = \frac{c_{\theta_0}^{(4)}(t)}{3[\langle \Delta(t) \rangle_{\theta_0}^2]^2}$$

vanishes with $t^2$ for $t \to 0$ and as $t^{-1}$ as $t \to \infty$. The angle-averaged non-Gaussian parameter,

$$\bar{p}(t) = \frac{c^{(4)}_{\theta_0}(t)}{3[\langle \Delta(t) \rangle^2]_0}$$

vanishes as $\frac{1}{\sqrt{t}}$, for $t \to 0$, and as $t^{-\frac{1}{2}}$ as $t \to \infty$. Because statistics in the body frame are Gaussian, the body-frame non-Gaussian parameter $p_{\theta_0}(t)$ is zero.

Equations 7 and 8 are confirmed numerically in Fig. 3A. Experimental measurements of both $p(t, \theta_0)$ and $\bar{p}(t)$ have poor statistics at large $t$ because their errors grow as $t^{-2}$. Nevertheless, we were able to extrapolate to the $t \to 0$ limit of $\bar{p}(t)$ in seven samples with different aspect ratios and to confirm Eq. 9 in the Fig. 3A inset. Figure 3A confirms our qualitative expectations about the non-Gaussian parameter $p$ in different frames and for different types of averages, specifically: (i) In the ensemble with fixed $\theta_0$, the non-Gaussian parameter vanishes for $t \gg \tau_0$ and $t \gg \tau_0$ and reaches a maximum when $t \sim \tau_0$; (ii) in the ensemble that averages over $\theta_0$, the non-Gaussian parameter is a maximum at $t = 0$ and vanishes for $t \gg \tau_0$; and (iii) larger $D_a/D_b$ causes larger non-Gaussian effects.

It is clear from Eqs. 6 to 9 that non-Gaussian behavior originates in particle anisotropy and vanishes when $\Delta D$ vanishes. Thus, non-Gaussian effects for anisotropic particles diffusing in 3D with stick boundary conditions should be small because $1 < D_a/D_b = \tau_q/\tau_0 < 2$ when $1 < a/b < \infty$ (5, 7). For some small molecules, the slip boundary condition is more appropriate (16, 17) and $\gamma_q/\gamma_0$ diverges ($\Pi$) even in 3D. Under quasi-2D conditions with stick boundary conditions, however, $D_a/D_b$ increases with aspect ratio and finally saturates (13) at a value much larger than 2. In summary, non-Gaussian effects are strong when $D_a > D_b$, i.e., for particles with a high aspect ratio confined in quasi-2D (in our case, $D_a/D_b$ reaches about 4) or for some molecules with slip boundary conditions.

Lastly, we consider the lab-frame PDF for $\Delta(t)$. The expectation is that these PDFs at fixed $\theta_0$ will be non-Gaussian and exhibit maximum deviations from Gaussian behavior at times of order $\tau_0$. We have verified that this is the case within our statistical errors, but the deviations are very small. The lab-frame PDF averaged over $\theta_0$ shows more striking deviations from Gaussian behavior (8), particularly as $t \to 0$:

$$f_{\Delta}(\Delta(t)) = \langle \delta(\Delta(t) - \xi(\Delta)) \rangle_{\theta_0} \approx \int_0^{2\pi} d\theta e^{i\Delta(t)\theta} / \sqrt{2\pi\sigma(t)}$$

where $\sigma(t)^2 = \sigma^2 \cos^2 \theta + \sigma_q^2 \sin^2 \theta$ with $\sigma_q^2 = 2D_q t$. The physical meaning of Eq. 10 is apparent. When $t \to 0$, the orientation $\theta$ does not change during the displacement. Those $\Delta(t)$ with the same $\theta(t)$ follow a Gaussian distribution with $\sigma = \sin(\theta(t))$ because the hydrodynamic drag coefficient $\gamma_q(\theta)$ is a constant. Averaging Gaussian PDFs with different $\theta_0$ over $[0,2\pi]$ yields a non-Gaussian PDF as shown in Eq. 10.

Experimental angle-averaged PDFs of lab-frame displacement are shown (Fig. 3B) at time intervals of $t = 0.1$ s. The system’s isotropy is confirmed by $f_{\Delta y}(x) = f_{\Delta x}(x)$. Interestingly, there are more tiny and large steps and fewer middle-sized steps than there are in a Gaussian distribution (fig. S2). This PDF agrees with Eq. 10 very well with no free parameters. We measured the PDFs of 15 samples with different aspect ratios at different confinements. All agreed with Eq. 10. When $D_a/D_b < 2.5$, the measured non-Gaussian PDF becomes indistinguishable from a Gaussian distribution.

The most common experimental probes typically measure only two moments, from which diffusion coefficients can be extracted, that provide no information about non-Gaussian behavior. For example, dynamic light scattering (12, 18) and nuclear magnetic resonance (NMR) (19) measure $\theta_0$-averaged translational diffusion coefficients of anisotropic constituents; and NMR (19), fluorescence depolarization (20), electric birefringence (21), dichroism (22), and depolarized dynamic light scattering (19) measure rotational diffusion coefficients. In principle, some of these probes, light scattering in particular, could provide a measure of $c^{(4)}_{\theta_0}(t) \to 3/2$ and higher moments, but we are not aware of any such measurements. Certainly, the non-Gaussian effects would be very small, especially for particles in 3D where $D_a/D_b < 2$.

Our observations using digital video microscopy of the Brownian motion of an isolated ellipsoid in two-dimensions provide exquisite detailed information about the diffusive properties of anisotropic objects and the subtle interplay between orientational and translational motions. Besides providing us with new insights about a fundamental phenomenon, these observations and underlying theory are potentially useful for research on diffusion of anisotropic molecules in membranes (16), on the hydrodynamics and kinetics of ensembles of anisotropic particles, and on anisotropic molecules that...
experience slip boundary conditions and thus have a large ratio of \( \gamma_2 \) to \( \gamma_1 \).

References and Notes
8. See the Supporting Online Materials of Science.

\[ \text{α-Hydroxy and α-Amino Acids Under Possible Hadean, Volcanic Origin-of-Life Conditions} \]

Claudia Huber1 and Günter Wächtershäuser2*†

To test the theory of a chemoenzymotrophic origin of life in a volcanic, hydrothermal setting, we explored mechanisms for the buildup of bio-organic compounds by carbon fixation on catalytic transition metal precipitates. We report the carbon monoxide-dependent formation of carbon-fixation products, including an ordered series of α-hydroxy and α-amino acids of the general formula R-CH(OH)COOH (where R is H, CH3, CH2OH, or HOCCH2) by carbon fixation at 80° to 120°C, catalyzed by nickel or nickel-iron precipitates with carbonyl, cyano, and methythiol ligands as carbon sources, with or without sulfido ligands. Calcium or magnesium hydroxide was added as a pH buffer. The results narrow the gap between biochemistry and volcanic geochemistry and open a new gateway for the exploration of a volcanic, hydrothermal origin of life.

To explore the theory of a volcanic, hydrothermal, chemoenzymotrophic origin of life, we postulate a locally and temporally coherent, evolvable system of autocatalytic, synthetic carbon fixation pathways, catalyzed by inorganic transition metal precipitates and generating low molecular weight organic compounds from highly oxidized precursors. Here, this system of pathways is termed “pioneer metabolism.” In accordance with the principle of metabolic continuity, the theory assumes a step-by-step evolutionary changeover by evolution of ligand feedback from racemic ligands of the inorganic transition metal precipitates to homochiral metalloenzymes of extant organisms. In a continuing effort to establish an experimental grounding for this hypothesis, we experimentally explored the viability of volcanic, hydrothermal carbon-fixation pathways using CO and CN− as carbon sources.

We chose Ni or Ni,Fe precipitates as catalytic transition metals because of the catalytic roles of these biometals (as sulfide or hydroxide complexes) in our previous experiments (5, 6; (Ca, Mg)(OH)2 as source for hydroxyl ligands and for buffering against acidification; Na2S or CH3-SNa as sources for sulfido or methythiol ligands; and CO and KCN as sources for carbonyl and cyano ligands in accordance with extant [Fe,Ni]- and [Fe,F]-hydrogenases (7).

The reaction conditions are listed in Table 1. Unless stated otherwise, the experiments were carried out in a slurry with 10 ml of H2O and 13C-labeled KCN (8). The alkaline pH range is 8.2 to 8.4, which suggests the participation of a pool of amino acids. The replacement of α-hydroxy- and α-amino acids as main products (Table 1) constitute ordered series defined by the general formula R-CH(OH)COOH, where R is H, CH3, CH2OH, or HO-CH2 and A is OH or NH2. Temperature increase correlates positively with product yield and with the ratio of amino acids to hydroxy acids. The replacement of H2O by D2O leads to deuterated products. With [13C]labeled KCN, we discriminated cyano ligands from CO and (optionally, methythiol) ligands as the carbon source. The resulting isotopomers revealed a rich and complex system of pathways involving alkyano, all-noncyano, and combined cyano/noncyano ligands, as exemplified by ratios of 12C/13C isotopomers for lactate and alanine. The contribution by noncyano pathways correlates positively with a decrease in CO gas pressure and an increase in temperature. This multiplicity of pathways may facilitate metabolic evolution and a stepwise changeover from a Ni-dependent use of CO and/or cyano ligands without energy coupling to a sole use of CO2 with energy coupling. We also detected α-hydroxy-n-valeric acid (run 4, 0.005 μmol), α-hydroxy-i-valeric acid (runs 4 and 5, trace amounts), and α-amino-n-valeric acid (run 4, trace amount). The progressive chain elongation suggests long-chain α-hydroxy or α-amino acids as primordial lipids.

Added 15N-NH3 enters the amino acids, which suggests the participation of a pool of ammonia. The replacement of KCl in run 3 by glycine and alanine generated α-hydroxy acids at very low rates. This means that α-amino and α-hydroxy acids are mainly competitive products and, to a minor extent, consecutive products. The detection of glycine amide by high-performance liquid chromatography (HPLC)–MS (8) suggests carboxamides as intermediates between CN and COOH groups. The detection of pyruvate (runs 3, 4, 5, and 10) having a similar isotopomer ratio as lactate and alanine suggests α-keto and α-imino groups as intermediates.

Acetate, propionate, and butyrate (in varying isotopomer ratios) have been detected with yields decreasing in that order. The detected ethylene...